

# Math 115—College Algebra

## Measurable Outcomes

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**Reference text:** Numbers in brackets refer to sections of Miller, O’Neill, and Hyde, *Intermediate Algebra*, fourth edition.

**Note:** Outcomes marked **(Optional)** may appear on the final exam with the unanimous consent of all instructors.

### 1. Linear equations in one variable

- 1(a) Distinguish linear from non-linear equations. [1.1]
- 1(b) Solve linear equations in one variable. [1.1]
- 1(c) **(Optional)** Model word problems with linear equations. [1.2]
- 1(d) Solve for one variable in a linear equation involving several variables. [1.3]

### 2. Linear inequalities in one variable

- 2(a) Solve linear inequalities in one variable. [1.4]
- 2(b) Describe unions and intersections of sets of real numbers. [1.5]
- 2(c) Solve systems of linear inequalities connected by “and” or “or.” [1.5]

### 3. Equations and inequalities with absolute values

- 3(a) Solve equations involving one or two absolute value expressions. [1.6]
- 3(b) Solve inequalities with one absolute value expression. [1.7]

### 4. Linear equations in two variables

- 4(a) Write a linear equation in standard form. [2.1]
- 4(b) Find the intercepts of a linear equation. [2.1]
- 4(c) Generate additional solutions of a linear equation. [2.1]
- 4(d) Recognize horizontal and vertical lines. [2.1]

- 4(e) Interpret slope as rise over run. [2.2]
- 4(f) Compute the slope of a line from two of its points. [2.2]
- 4(g) Recognize parallel and perpendicular lines by comparing their slopes. [2.2]
- 4(h) Write a linear equation in slope-intercept form. [2.3]
- 4(i) Graph a linear equation in slope-intercept form. [2.3]
- 4(j) Find the equation of a line, given its slope and  $y$ -intercept. [2.3]
- 4(k) Use the point-slope form to find the equation of a line, given its slope and one point. [2.3]
- 4(l) Find the equation of a line, given two points. [2.3]
- 4(m) Write the equation of a line parallel or perpendicular to a given line, through a given point. [2.3]
- 4(n) **(Optional)** Model word problems using linear equations in two variables. [2.4]

## 5. Relations and functions

- 5(a) Write a relation as a set of ordered pairs. [2.5]
- 5(b) Describe the domain and range of a relation. [2.5]
- 5(c) Distinguish functions from more general relations. [2.6]
- 5(d) Recognize the graph of a function using the Vertical Line Test. [2.6]
- 5(e) Use function notation. [2.6]
- 5(f) Read function values from a graph. [2.6]
- 5(g) Find the largest possible domain of a function, given a formula for the function. [2.6]
- 5(h) Recognize constant, linear, and quadratic functions. [2.7]
- 5(i) Reproduce the graphs of the identity, squaring, cubing, absolute value, square root, and reciprocal functions. [2.7]
- 5(j) Find the  $x$ - and  $y$ -intercepts of a function, given a formula for the function. [2.7]

## 6. Systems of linear equations

- 6(a) Determine whether a point is a solution of a system of equations. [3.1]
- 6(b) Solve a linear system by graphing. [3.1]
- 6(c) Solve a linear system using the Substitution Method. [3.2]

- 6(d)** Solve a linear system using the Addition Method (i.e. the Elimination Method). [3.3]
- 6(e)** Recognize inconsistent and dependent systems. [3.2, 3.3]
- 6(f) (Optional)** Model word problems with linear systems. [3.4]

## 7. Polynomials

- 7(a)** Simplify expressions using the laws of exponents. [4.1]
- 7(b)** Use scientific notation. [4.1]
- 7(c)** Recognize monomial, binomial, trinomial, and polynomial expressions [4.2]
- 7(d)** Add and subtract polynomial expressions. [4.2]
- 7(e)** Recognize the degree of a polynomial expression. [4.2]
- 7(f) (Optional)** Model word problems with polynomial functions. [4.2]
- 7(g)** Multiply polynomials. [4.3]
- 7(h)** Square a binomial. [4.3]
- 7(i) (Optional)** Cube a binomial. [4.3]
- 7(j) (Optional)** Divide a polynomial by a monomial. [4.4]
- 7(k) (Optional)** Compute quotient and remainder using polynomial long division. [4.4]
- 7(l)** Find the greatest common factor of several monomials. [4.5]
- 7(m)** Factor the greatest common factor out of a polynomial. [4.5]
- 7(n)** Factor a polynomial by grouping. [4.5]
- 7(o)** Factor trinomials. [4.6]
- 7(p)** Recognize and factor perfect square trinomials. [4.7]
- 7(q)** Factor a difference of squares. [4.7]
- 7(r) (Optional)** Factor a sum or difference of cubes. [4.7]
- 7(s)** Write and explain the zero-product rule [4.8]
- 7(t)** Solve polynomial equations by factoring. [4.8]

## 8. Rational expressions

- 8(a)** Distinguish rational expressions from more general expressions. [5.1]
- 8(b)** Reduce a rational expression to lowest terms. [5.1]
- 8(c)** Multiply and divide rational expressions. [5.2]
- 8(d)** Find the least common denominator of two rational expressions. [5.3]

- 8(e) Add and subtract rational expressions. [5.3]
- 8(f) Reduce compound fractions. [5.4]
- 8(g) Solve a rational equation in one variable. [5.5]
- 8(h) Solve for one variable in a rational equation with several variables. [5.5]
- 8(i) **(Optional)** Solve proportions and similar triangles. [5.6]
- 8(j) **(Optional)** Recognize direct and inverse variation. [5.7]

## 9. Radicals

- 9(a) Correctly interpret and evaluate  $\sqrt{a}$  (the *principal* or non-negative square root of a non-negative real number  $a$ ). [6.1]
- 9(b) Find all real solutions of equations of the form  $x^2 = a$ . [6.1]
- 9(c) Correctly interpret and evaluate  $\sqrt[n]{a}$ , where  $n$  is any positive integer and  $a$  is a non-negative real number. [6.1]
- 9(d) Find all real solutions of equations of the form  $x^n = a$ . [6.1]
- 9(e) Simplify expressions of the form  $\sqrt[n]{a^n}$ . [6.1]
- 9(f) Find the third side of a right triangle, given any two sides. [6.1]
- 9(g) Find the largest possible domain of a function involving radicals. [6.1]
- 9(h) Evaluate expressions of the form  $a^{n/m}$ . [6.2]
- 9(i) Convert between radical notation and rational exponents. [6.2]
- 9(j) Simplify expressions involving rational exponents by using the laws of exponents. [6.3]
- 9(k) Simplify radical expressions using the fact that  $\sqrt[n]{ab} = \sqrt[n]{a} \sqrt[n]{b}$  when  $a, b > 0$ . [6.3]
- 9(l) Add and subtract radical expressions. [6.4]
- 9(m) Multiply radical expressions. [6.5]
- 9(n) Multiply radicals with different indices. [6.5]
- 9(o) Simplify radical expressions using the fact that  $\sqrt[n]{a/b} = \sqrt[n]{a} / \sqrt[n]{b}$  when  $a, b > 0$ . [6.6]
- 9(p) Rationalize the denominator of a radical expression. [6.6]
- 9(q) Solve equations involving one or two radical expressions. [6.7]

## 10. Quadratic equations and quadratic functions

- 10(a) Solve quadratic equations by completing the square. [7.1]

- 10(b) Solve quadratic equations by using the Quadratic Formula. [7.2]
- 10(c) Calculate the discriminant of a quadratic expression. [7.2]
- 10(d) Use the discriminant to predict the number of real solutions of a quadratic equation. [7.2]
- 10(e) **(Optional)** Solve equations in quadratic form. [7.3]
- 10(f) Sketch the graph of a quadratic function. [7.4]
- 10(g) Find the vertex of a parabola. [7.5]
- 10(h) Solve quadratic optimization problems. [7.5]

## 11. Polynomial and rational inequalities (Optional)

- 11(a) **(Optional)** Solve polynomial inequalities. [7.6]
- 11(b) **(Optional)** Solve rational inequalities. [7.6]